

**UCL Statistics for Uncensored Full Data Sets**

User Selected Options  
 Date/Time of Computation ProUCL 5.18/23/2017 11:42:10 AM  
 From File Input.xls  
 Full Precision OFF  
 Confidence Coefficient 95%  
 Number of Bootstrap Operations 10000

**final\_numeric (radium-226)**

**General Statistics**

Total Number of Observations	58	Number of Distinct Observations	50
		Number of Missing Observations	0
Minimum	0.426	Mean	1.26
Maximum	2.46	Median	1.2
SD	0.44	Std. Error of Mean	0.0578
Coefficient of Variation	0.349	Skewness	0.852

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.942	<b>Shapiro Wilk GOF Test</b>
5% Shapiro Wilk P Value	0.0128	Data Not Normal at 5% Significance Level
Lilliefors Test Statistic	0.121	<b>Lilliefors GOF Test</b>
5% Lilliefors Critical Value	0.116	Data Not Normal at 5% Significance Level

**Data Not Normal at 5% Significance Level**

**Assuming Normal Distribution**

**95% Normal UCL**

95% Student's-t UCL 1.357

**95% UCLs (Adjusted for Skewness)**

95% Adjusted-CLT UCL (Chen-1995) 1.362  
 95% Modified-t UCL (Johnson-1978) 1.358

**Gamma GOF Test**

A-D Test Statistic	0.278	<b>Anderson-Darling Gamma GOF Test</b>
5% A-D Critical Value	0.752	Detected data appear Gamma Distributed at 5% Significance Level
K-S Test Statistic	0.0759	<b>Kolmogorov-Smirnov Gamma GOF Test</b>
5% K-S Critical Value	0.117	Detected data appear Gamma Distributed at 5% Significance Level

**Detected data appear Gamma Distributed at 5% Significance Level**

**Gamma Statistics**

k hat (MLE)	8.671	k star (bias corrected MLE)	8.234
Theta hat (MLE)	0.145	Theta star (bias corrected MLE)	0.153
nu hat (MLE)	1006	nu star (bias corrected)	955.1
MLE Mean (bias corrected)	1.26	MLE Sd (bias corrected)	0.439
		Approximate Chi Square Value (0.05)	884.4
Adjusted Level of Significance	0.0459	Adjusted Chi Square Value	882.7

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50) 1.361

95% Adjusted Gamma UCL (use when n<50) 1.364

**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.983	<b>Shapiro Wilk Lognormal GOF Test</b>
5% Shapiro Wilk P Value	0.794	Data appear Lognormal at 5% Significance Level
Lilliefors Test Statistic	0.0544	<b>Lilliefors Lognormal GOF Test</b>
5% Lilliefors Critical Value	0.116	Data appear Lognormal at 5% Significance Level

**Data appear Lognormal at 5% Significance Level**

**Lognormal Statistics**

Minimum of Logged Data	-0.853	Mean of logged Data	0.173
Maximum of Logged Data	0.9	SD of logged Data	0.35

**Assuming Lognormal Distribution**

95% H-UCL	1.369	90% Chebyshev (MVUE) UCL	1.44
95% Chebyshev (MVUE) UCL	1.521	97.5% Chebyshev (MVUE) UCL	1.633
99% Chebyshev (MVUE) UCL	1.854		

**Nonparametric Distribution Free UCL Statistics**

**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**

95% CLT UCL	1.355	95% Jackknife UCL	1.357
95% Standard Bootstrap UCL	1.356	95% Bootstrap-t UCL	1.363

95% Hall's Bootstrap UCL	1.364	95% Percentile Bootstrap UCL	1.358
95% BCA Bootstrap UCL	1.361		
90% Chebyshev(Mean, Sd) UCL	1.434	95% Chebyshev(Mean, Sd) UCL	1.512
97.5% Chebyshev(Mean, Sd) UCL	1.621	99% Chebyshev(Mean, Sd) UCL	1.835

**Suggested UCL to Use**

95% Approximate Gamma UCL 1.361

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL.

Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (radium-228)

**General Statistics**

Total Number of Observations	58	Number of Distinct Observations	42
		Number of Missing Observations	0
Minimum	0.875	Mean	1.604
Maximum	3.01	Median	1.565
SD	0.357	Std. Error of Mean	0.0469
Coefficient of Variation	0.223	Skewness	1.087

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.946
5% Shapiro Wilk P Value	0.0212
Lilliefors Test Statistic	0.119
5% Lilliefors Critical Value	0.116

**Shapiro Wilk GOF Test**

Data Not Normal at 5% Significance Level

**Lilliefors GOF Test**

Data Not Normal at 5% Significance Level

**Data Not Normal at 5% Significance Level**

**Assuming Normal Distribution**

**95% Normal UCL**

95% Student's-t UCL 1.683

**95% UCLs (Adjusted for Skewness)**

95% Adjusted-CLT UCL (Chen-1995)	1.689
95% Modified-t UCL (Johnson-1978)	1.684

**Gamma GOF Test**

A-D Test Statistic	0.414
5% A-D Critical Value	0.749
K-S Test Statistic	0.0915
5% K-S Critical Value	0.117

**Anderson-Darling Gamma GOF Test**

Detected data appear Gamma Distributed at 5% Significance Level

**Kolmogorov-Smirnov Gamma GOF Test**

Detected data appear Gamma Distributed at 5% Significance Level

**Detected data appear Gamma Distributed at 5% Significance Level**

**Gamma Statistics**

k hat (MLE)	21.84	k star (bias corrected MLE)	20.72
Theta hat (MLE)	0.0735	Theta star (bias corrected MLE)	0.0774
nu hat (MLE)	2533	nu star (bias corrected)	2403
MLE Mean (bias corrected)	1.604	MLE Sd (bias corrected)	0.352
Adjusted Level of Significance	0.0459	Approximate Chi Square Value (0.05)	2290
		Adjusted Chi Square Value	2288

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50) 1.683

95% Adjusted Gamma UCL (use when n<50) 1.685

**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.988
5% Shapiro Wilk P Value	0.941
Lilliefors Test Statistic	0.0873
5% Lilliefors Critical Value	0.116

**Shapiro Wilk Lognormal GOF Test**

Data appear Lognormal at 5% Significance Level

**Lilliefors Lognormal GOF Test**

Data appear Lognormal at 5% Significance Level

**Data appear Lognormal at 5% Significance Level**

**Lognormal Statistics**

Minimum of Logged Data	-0.134	Mean of logged Data	0.45
Maximum of Logged Data	1.102	SD of logged Data	0.216

**Assuming Lognormal Distribution**

95% H-UCL	1.685	90% Chebyshev (MVUE) UCL	1.741
95% Chebyshev (MVUE) UCL	1.804	97.5% Chebyshev (MVUE) UCL	1.89
99% Chebyshev (MVUE) UCL	2.06		

**Nonparametric Distribution Free UCL Statistics**

**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**

95% CLT UCL	1.681	95% Jackknife UCL	1.683
95% Standard Bootstrap UCL	1.682	95% Bootstrap-t UCL	1.692
95% Hall's Bootstrap UCL	1.697	95% Percentile Bootstrap UCL	1.682
95% BCA Bootstrap UCL	1.689		
90% Chebyshev(Mean, Sd) UCL	1.745	95% Chebyshev(Mean, Sd) UCL	1.809
97.5% Chebyshev(Mean, Sd) UCL	1.897	99% Chebyshev(Mean, Sd) UCL	2.071

**Suggested UCL to Use**

95% Approximate Gamma UCL 1.683

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL.

Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006).

However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (thorium-228)

**General Statistics**

Total Number of Observations	55	Number of Distinct Observations	46
		Number of Missing Observations	0
Minimum	1.21	Mean	1.949
Maximum	3.04	Median	1.88
SD	0.387	Std. Error of Mean	0.0522
Coefficient of Variation	0.199	Skewness	0.796

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.954
5% Shapiro Wilk P Value	0.0671
Lilliefors Test Statistic	0.103
5% Lilliefors Critical Value	0.119

**Shapiro Wilk GOF Test**

Data appear Normal at 5% Significance Level

**Lilliefors GOF Test**

Data appear Normal at 5% Significance Level

Data appear Normal at 5% Significance Level

**Assuming Normal Distribution**

**95% Normal UCL**

95% Student's-t UCL 2.036

**95% UCLs (Adjusted for Skewness)**

95% Adjusted-CLT UCL (Chen-1995)	2.041
95% Modified-t UCL (Johnson-1978)	2.037

**Gamma GOF Test**

A-D Test Statistic	0.351
5% A-D Critical Value	0.748
K-S Test Statistic	0.078
5% K-S Critical Value	0.12

**Anderson-Darling Gamma GOF Test**

Detected data appear Gamma Distributed at 5% Significance Level

**Kolmogorov-Smirnov Gamma GOF Test**

Detected data appear Gamma Distributed at 5% Significance Level

Detected data appear Gamma Distributed at 5% Significance Level

**Gamma Statistics**

k hat (MLE)	27.19	k star (bias corrected MLE)	25.71
Theta hat (MLE)	0.0717	Theta star (bias corrected MLE)	0.0758
nu hat (MLE)	2990	nu star (bias corrected)	2829
MLE Mean (bias corrected)	1.949	MLE Sd (bias corrected)	0.384
Adjusted Level of Significance	0.0456	Approximate Chi Square Value (0.05)	2706
		Adjusted Chi Square Value	2703

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50))	2.037	95% Adjusted Gamma UCL (use when n<50)	2.039
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**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.986
5% Shapiro Wilk P Value	0.9
Lilliefors Test Statistic	0.0686
5% Lilliefors Critical Value	0.119

**Shapiro Wilk Lognormal GOF Test**

Data appear Lognormal at 5% Significance Level

**Lilliefors Lognormal GOF Test**

Data appear Lognormal at 5% Significance Level

Data appear Lognormal at 5% Significance Level

**Lognormal Statistics**

Minimum of Logged Data	0.191	Mean of logged Data	0.649
Maximum of Logged Data	1.112	SD of logged Data	0.193

**Assuming Lognormal Distribution**

95% H-UCL	2.039	90% Chebyshev (MVUE) UCL	2.101
95% Chebyshev (MVUE) UCL	2.171	97.5% Chebyshev (MVUE) UCL	2.267

99% Chebyshev (MVUE) UCL 2.456

**Nonparametric Distribution Free UCL Statistics**

**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**

95% CLT UCL	2.035	95% Jackknife UCL	2.036
95% Standard Bootstrap UCL	2.033	95% Bootstrap-t UCL	2.044
95% Hall's Bootstrap UCL	2.04	95% Percentile Bootstrap UCL	2.034
95% BCA Bootstrap UCL	2.043		
90% Chebyshev(Mean, Sd) UCL	2.105	95% Chebyshev(Mean, Sd) UCL	2.176
97.5% Chebyshev(Mean, Sd) UCL	2.275	99% Chebyshev(Mean, Sd) UCL	2.468

**Suggested UCL to Use**

95% Student's-t UCL 2.036

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (thorium-230)

**General Statistics**

Total Number of Observations	55	Number of Distinct Observations	46
		Number of Missing Observations	0
Minimum	0.782	Mean	1.427
Maximum	3.03	Median	1.29
SD	0.523	Std. Error of Mean	0.0705
Coefficient of Variation	0.366	Skewness	1.657

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.826	<b>Shapiro Wilk GOF Test</b>
5% Shapiro Wilk P Value	1.7983E-8	Data Not Normal at 5% Significance Level
Lilliefors Test Statistic	0.193	<b>Lilliefors GOF Test</b>
5% Lilliefors Critical Value	0.119	Data Not Normal at 5% Significance Level

**Data Not Normal at 5% Significance Level**

**Assuming Normal Distribution**

<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.544	95% Adjusted-CLT UCL (Chen-1995)	1.559
		95% Modified-t UCL (Johnson-1978)	1.547

**Gamma GOF Test**

A-D Test Statistic	1.475	<b>Anderson-Darling Gamma GOF Test</b>
5% A-D Critical Value	0.751	Data Not Gamma Distributed at 5% Significance Level
K-S Test Statistic	0.144	<b>Kolmogorov-Smirnov Gamma GOF Test</b>
5% K-S Critical Value	0.12	Data Not Gamma Distributed at 5% Significance Level

**Data Not Gamma Distributed at 5% Significance Level**

**Gamma Statistics**

k hat (MLE)	9.434	k star (bias corrected MLE)	8.931
Theta hat (MLE)	0.151	Theta star (bias corrected MLE)	0.16
nu hat (MLE)	1038	nu star (bias corrected)	982.4
MLE Mean (bias corrected)	1.427	MLE Sd (bias corrected)	0.477
		Approximate Chi Square Value (0.05)	910.7
Adjusted Level of Significance	0.0456	Adjusted Chi Square Value	908.8

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50))	1.539	95% Adjusted Gamma UCL (use when n<50)	1.542
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**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.936	<b>Shapiro Wilk Lognormal GOF Test</b>
5% Shapiro Wilk P Value	0.00816	Data Not Lognormal at 5% Significance Level
Lilliefors Test Statistic	0.12	<b>Lilliefors Lognormal GOF Test</b>
5% Lilliefors Critical Value	0.119	Data Not Lognormal at 5% Significance Level

**Data Not Lognormal at 5% Significance Level**

**Lognormal Statistics**

Minimum of Logged Data	-0.246	Mean of logged Data	0.301
Maximum of Logged Data	1.109	SD of logged Data	0.318

<b>Assuming Lognormal Distribution</b>			
95% H-UCL	1.532	90% Chebyshev (MVUE) UCL	1.607
95% Chebyshev (MVUE) UCL	1.692	97.5% Chebyshev (MVUE) UCL	1.81
99% Chebyshev (MVUE) UCL	2.04		

**Nonparametric Distribution Free UCL Statistics**  
**Data do not follow a Discernible Distribution (0.05)**

<b>Nonparametric Distribution Free UCLs</b>			
95% CLT UCL	1.542	95% Jackknife UCL	1.544
95% Standard Bootstrap UCL	1.541	95% Bootstrap-t UCL	1.567
95% Hall's Bootstrap UCL	1.569	95% Percentile Bootstrap UCL	1.545
95% BCA Bootstrap UCL	1.559		
90% Chebyshev(Mean, Sd) UCL	1.638	95% Chebyshev(Mean, Sd) UCL	1.734
97.5% Chebyshev(Mean, Sd) UCL	1.867	99% Chebyshev(Mean, Sd) UCL	2.128

<b>Suggested UCL to Use</b>			
95% Student's-t UCL	1.544	or 95% Modified-t UCL	1.547

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (thorium-232)

<b>General Statistics</b>			
Total Number of Observations	55	Number of Distinct Observations	46
		Number of Missing Observations	0
Minimum	1.05	Mean	1.774
Maximum	2.74	Median	1.78
SD	0.367	Std. Error of Mean	0.0495
Coefficient of Variation	0.207	Skewness	0.189
<b>Normal GOF Test</b>			
Shapiro Wilk Test Statistic	0.981	<b>Shapiro Wilk GOF Test</b>	
5% Shapiro Wilk P Value	0.721	Data appear Normal at 5% Significance Level	
Lilliefors Test Statistic	0.0597	<b>Lilliefors GOF Test</b>	
5% Lilliefors Critical Value	0.119	Data appear Normal at 5% Significance Level	
<b>Data appear Normal at 5% Significance Level</b>			

<b>Assuming Normal Distribution</b>			
<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.857	95% Adjusted-CLT UCL (Chen-1995)	1.857
		95% Modified-t UCL (Johnson-1978)	1.857

<b>Gamma GOF Test</b>			
A-D Test Statistic	0.333	<b>Anderson-Darling Gamma GOF Test</b>	
5% A-D Critical Value	0.748	Detected data appear Gamma Distributed at 5% Significance Level	
K-S Test Statistic	0.0761	<b>Kolmogorov-Smirnov Gamma GOF Test</b>	
5% K-S Critical Value	0.12	Detected data appear Gamma Distributed at 5% Significance Level	
<b>Detected data appear Gamma Distributed at 5% Significance Level</b>			

<b>Gamma Statistics</b>			
k hat (MLE)	23.17	k star (bias corrected MLE)	21.92
Theta hat (MLE)	0.0766	Theta star (bias corrected MLE)	0.0809
nu hat (MLE)	2549	nu star (bias corrected)	2411
MLE Mean (bias corrected)	1.774	MLE Sd (bias corrected)	0.379
		Approximate Chi Square Value (0.05)	2298
Adjusted Level of Significance	0.0456	Adjusted Chi Square Value	2295

<b>Assuming Gamma Distribution</b>			
95% Approximate Gamma UCL (use when n>=50)	1.861	95% Adjusted Gamma UCL (use when n<50)	1.863

<b>Lognormal GOF Test</b>			
Shapiro Wilk Test Statistic	0.973	<b>Shapiro Wilk Lognormal GOF Test</b>	
5% Shapiro Wilk P Value	0.434	Data appear Lognormal at 5% Significance Level	
Lilliefors Test Statistic	0.0903	<b>Lilliefors Lognormal GOF Test</b>	
5% Lilliefors Critical Value	0.119	Data appear Lognormal at 5% Significance Level	
<b>Data appear Lognormal at 5% Significance Level</b>			

Lognormal Statistics			
Minimum of Logged Data	0.0488	Mean of logged Data	0.551
Maximum of Logged Data	1.008	SD of logged Data	0.213

Assuming Lognormal Distribution			
95% H-UCL	1.866	90% Chebyshev (MVUE) UCL	1.929
95% Chebyshev (MVUE) UCL	1.999	97.5% Chebyshev (MVUE) UCL	2.096
99% Chebyshev (MVUE) UCL	2.287		

**Nonparametric Distribution Free UCL Statistics**  
**Data appear to follow a Discernible Distribution at 5% Significance Level**

Nonparametric Distribution Free UCLs			
95% CLT UCL	1.855	95% Jackknife UCL	1.857
95% Standard Bootstrap UCL	1.855	95% Bootstrap-t UCL	1.859
95% Hall's Bootstrap UCL	1.858	95% Percentile Bootstrap UCL	1.856
95% BCA Bootstrap UCL	1.853		
90% Chebyshev(Mean, Sd) UCL	1.922	95% Chebyshev(Mean, Sd) UCL	1.989
97.5% Chebyshev(Mean, Sd) UCL	2.083	99% Chebyshev(Mean, Sd) UCL	2.266

**Suggested UCL to Use**  
**95% Student's-t UCL 1.857**

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness. These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (uranium-234)

General Statistics			
Total Number of Observations	55	Number of Distinct Observations	47
		Number of Missing Observations	0
Minimum	0.775	Mean	1.515
Maximum	3.52	Median	1.24
SD	0.69	Std. Error of Mean	0.093
Coefficient of Variation	0.455	Skewness	1.417

Normal GOF Test		Shapiro Wilk GOF Test	
Shapiro Wilk Test Statistic	0.814	Data Not Normal at 5% Significance Level	
5% Shapiro Wilk P Value	5.2632E-9	<b>Lilliefors GOF Test</b>	
Lilliefors Test Statistic	0.21	Data Not Normal at 5% Significance Level	
5% Lilliefors Critical Value	0.119		

**Data Not Normal at 5% Significance Level**

Assuming Normal Distribution			
<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.671	95% Adjusted-CLT UCL (Chen-1995)	1.687
		95% Modified-t UCL (Johnson-1978)	1.674

Gamma GOF Test		Anderson-Darling Gamma GOF Test	
A-D Test Statistic	2.26	Data Not Gamma Distributed at 5% Significance Level	
5% A-D Critical Value	0.753	<b>Kolmogorov-Smirnov Gamma GOF Test</b>	
K-S Test Statistic	0.182	Data Not Gamma Distributed at 5% Significance Level	
5% K-S Critical Value	0.12		

**Data Not Gamma Distributed at 5% Significance Level**

Gamma Statistics			
k hat (MLE)	6.172	k star (bias corrected MLE)	5.848
Theta hat (MLE)	0.245	Theta star (bias corrected MLE)	0.259
nu hat (MLE)	679	nu star (bias corrected)	643.3
MLE Mean (bias corrected)	1.515	MLE Sd (bias corrected)	0.627
		Approximate Chi Square Value (0.05)	585.4
Adjusted Level of Significance	0.0456	Adjusted Chi Square Value	584

Assuming Gamma Distribution			
95% Approximate Gamma UCL (use when n>=50)	1.665	95% Adjusted Gamma UCL (use when n<50)	1.669

Lognormal GOF Test		Shapiro Wilk Lognormal GOF Test	
Shapiro Wilk Test Statistic	0.907		

5% Shapiro Wilk P Value	2.3394E-4	Data Not Lognormal at 5% Significance Level
Lilliefors Test Statistic	0.16	<b>Lilliefors Lognormal GOF Test</b>
5% Lilliefors Critical Value	0.119	Data Not Lognormal at 5% Significance Level

**Data Not Lognormal at 5% Significance Level**

Lognormal Statistics			
Minimum of Logged Data	-0.255	Mean of logged Data	0.332
Maximum of Logged Data	1.258	SD of logged Data	0.393

Assuming Lognormal Distribution			
95% H-UCL	1.659	90% Chebyshev (MVUE) UCL	1.751
95% Chebyshev (MVUE) UCL	1.863	97.5% Chebyshev (MVUE) UCL	2.019
99% Chebyshev (MVUE) UCL	2.324		

**Nonparametric Distribution Free UCL Statistics**  
**Data do not follow a Discernible Distribution (0.05)**

Nonparametric Distribution Free UCLs			
95% CLT UCL	1.668	95% Jackknife UCL	1.671
95% Standard Bootstrap UCL	1.667	95% Bootstrap-t UCL	1.695
95% Hall's Bootstrap UCL	1.691	95% Percentile Bootstrap UCL	1.668
95% BCA Bootstrap UCL	1.681		
90% Chebyshev(Mean, Sd) UCL	1.794	95% Chebyshev(Mean, Sd) UCL	1.921
97.5% Chebyshev(Mean, Sd) UCL	2.096	99% Chebyshev(Mean, Sd) UCL	2.441

Suggested UCL to Use			
95% Student's-t UCL	1.671	or 95% Modified-t UCL	1.674

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness. These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (uranium-235)

General Statistics			
Total Number of Observations	58	Number of Distinct Observations	57
		Number of Missing Observations	0
Minimum	-0.00891	Mean	0.0627
Maximum	0.198	Median	0.0545
SD	0.0422	Std. Error of Mean	0.00554
Coefficient of Variation	0.674	Skewness	1.502

Normal GOF Test		Shapiro Wilk GOF Test	
Shapiro Wilk Test Statistic	0.865	Data Not Normal at 5% Significance Level	
5% Shapiro Wilk P Value	7.1862E-7	<b>Lilliefors GOF Test</b>	
Lilliefors Test Statistic	0.187	Data Not Normal at 5% Significance Level	
5% Lilliefors Critical Value	0.116		

**Data Not Normal at 5% Significance Level**

Assuming Normal Distribution		95% UCLs (Adjusted for Skewness)	
95% Normal UCL		95% Adjusted-CLT UCL (Chen-1995)	0.0729
95% Student's-t UCL	0.0719	95% Modified-t UCL (Johnson-1978)	0.0721

**Gamma Statistics Not Available**  
**Lognormal Statistics Not Available**

**Nonparametric Distribution Free UCL Statistics**  
**Data do not follow a Discernible Distribution (0.05)**

Nonparametric Distribution Free UCLs			
95% CLT UCL	0.0718	95% Jackknife UCL	0.0719
95% Standard Bootstrap UCL	0.0718	95% Bootstrap-t UCL	0.0734
95% Hall's Bootstrap UCL	0.0736	95% Percentile Bootstrap UCL	0.0721
95% BCA Bootstrap UCL	0.073		
90% Chebyshev(Mean, Sd) UCL	0.0793	95% Chebyshev(Mean, Sd) UCL	0.0868
97.5% Chebyshev(Mean, Sd) UCL	0.0973	99% Chebyshev(Mean, Sd) UCL	0.118

Suggested UCL to Use	
95% Chebyshev (Mean, Sd) UCL	0.0868

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

**final\_numeric (uranium-238)**

<b>General Statistics</b>			
Total Number of Observations	58	Number of Distinct Observations	46
		Number of Missing Observations	0
Minimum	0	Mean	1.321
Maximum	2.6	Median	1.205
SD	0.489	Std. Error of Mean	0.0642
Coefficient of Variation	0.37	Skewness	1.011
<b>Normal GOF Test</b>			
Shapiro Wilk Test Statistic	0.864	<b>Shapiro Wilk GOF Test</b>	
5% Shapiro Wilk P Value	5.7877E-7	Data Not Normal at 5% Significance Level	
Lilliefors Test Statistic	0.2	<b>Lilliefors GOF Test</b>	
5% Lilliefors Critical Value	0.116	Data Not Normal at 5% Significance Level	
<b>Data Not Normal at 5% Significance Level</b>			
<b>Assuming Normal Distribution</b>			
<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.428	95% Adjusted-CLT UCL (Chen-1995)	1.436
		95% Modified-t UCL (Johnson-1978)	1.43
<b>Gamma Statistics Not Available</b>			
<b>Lognormal Statistics Not Available</b>			
<b>Nonparametric Distribution Free UCL Statistics</b>			
<b>Data do not follow a Discernible Distribution (0.05)</b>			
<b>Nonparametric Distribution Free UCLs</b>			
95% CLT UCL	1.427	95% Jackknife UCL	1.428
95% Standard Bootstrap UCL	1.425	95% Bootstrap-t UCL	1.44
95% Hall's Bootstrap UCL	1.438	95% Percentile Bootstrap UCL	1.43
95% BCA Bootstrap UCL	1.438		
90% Chebyshev(Mean, Sd) UCL	1.514	<b>95% Chebyshev(Mean, Sd) UCL</b>	<b>1.601</b>
97.5% Chebyshev(Mean, Sd) UCL	1.722	99% Chebyshev(Mean, Sd) UCL	1.96
<b>Suggested UCL to Use</b>			
95% Chebyshev (Mean, Sd) UCL	1.601		

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.



### UCL Statistics for Uncensored Full Data Sets

User Selected Options  
 Date/Time of Computation ProUCL 5.110/2/2017 10:52:31 AM  
 From File Input.xls  
 Full Precision OFF  
 Confidence Coefficient 95%  
 Number of Bootstrap Operations 10000

final\_numeric (brc/timet\_radium-226)

General Statistics			
Total Number of Observations	104	Number of Distinct Observations	82
		Number of Missing Observations	0
Minimum	0.494	Mean	1.112
Maximum	2.36	Median	1.065
SD	0.347	Std. Error of Mean	0.0341
Coefficient of Variation	0.312	Skewness	0.987

Normal GOF Test		Shapiro Wilk GOF Test	
Shapiro Wilk Test Statistic	0.938	Data Not Normal at 5% Significance Level	
5% Shapiro Wilk P Value	1.0574E-4		
Lilliefors Test Statistic	0.111	Lilliefors GOF Test	
5% Lilliefors Critical Value	0.0872	Data Not Normal at 5% Significance Level	

**Data Not Normal at 5% Significance Level**

Assuming Normal Distribution			
<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.169	95% Adjusted-CLT UCL (Chen-1995)	1.172
		95% Modified-t UCL (Johnson-1978)	1.169

Gamma GOF Test		Anderson-Darling Gamma GOF Test	
A-D Test Statistic	0.643	Detected data appear Gamma Distributed at 5% Significance Level	
5% A-D Critical Value	0.752	Kolmogorov-Smirnov Gamma GOF Test	
K-S Test Statistic	0.071	Detected data appear Gamma Distributed at 5% Significance Level	
5% K-S Critical Value	0.0884	<b>Detected data appear Gamma Distributed at 5% Significance Level</b>	

Gamma Statistics			
k hat (MLE)	11.02	k star (bias corrected MLE)	10.71
Theta hat (MLE)	0.101	Theta star (bias corrected MLE)	0.104
nu hat (MLE)	2292	nu star (bias corrected)	2227
MLE Mean (bias corrected)	1.112	MLE Sd (bias corrected)	0.34
		Approximate Chi Square Value (0.05)	2118
Adjusted Level of Significance	0.0477	Adjusted Chi Square Value	2117

Assuming Gamma Distribution			
<b>95% Approximate Gamma UCL (use when n&gt;=50)</b>	<b>1.169</b>	<b>95% Adjusted Gamma UCL (use when n&lt;50)</b>	<b>1.17</b>

Lognormal GOF Test		Shapiro Wilk Lognormal GOF Test	
Shapiro Wilk Test Statistic	0.979	Data appear Lognormal at 5% Significance Level	
5% Shapiro Wilk P Value	0.468		
Lilliefors Test Statistic	0.0658	Lilliefors Lognormal GOF Test	
5% Lilliefors Critical Value	0.0872	Data appear Lognormal at 5% Significance Level	

**Data appear Lognormal at 5% Significance Level**

Lognormal Statistics			
Minimum of Logged Data	-0.705	Mean of logged Data	0.0603
Maximum of Logged Data	0.859	SD of logged Data	0.305

Assuming Lognormal Distribution			
95% H-UCL	1.173	90% Chebyshev (MVUE) UCL	1.214
95% Chebyshev (MVUE) UCL	1.261	97.5% Chebyshev (MVUE) UCL	1.325
99% Chebyshev (MVUE) UCL	1.451		

**Nonparametric Distribution Free UCL Statistics**  
**Data appear to follow a Discernible Distribution at 5% Significance Level**

Nonparametric Distribution Free UCLs			
95% CLT UCL	1.168	95% Jackknife UCL	1.169
95% Standard Bootstrap UCL	1.167	95% Bootstrap-t UCL	1.174

95% Hall's Bootstrap UCL	1.173	95% Percentile Bootstrap UCL	1.168
95% BCA Bootstrap UCL	1.172		
90% Chebyshev(Mean, Sd) UCL	1.214	95% Chebyshev(Mean, Sd) UCL	1.261
97.5% Chebyshev(Mean, Sd) UCL	1.325	99% Chebyshev(Mean, Sd) UCL	1.451

**Suggested UCL to Use**

95% Approximate Gamma UCL 1.169

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (brc/timet\_radium-228)

General Statistics			
Total Number of Observations	84	Number of Distinct Observations	66
		Number of Missing Observations	0
Minimum	0.946	Mean	1.916
Maximum	2.94	Median	1.96
SD	0.405	Std. Error of Mean	0.0441
Coefficient of Variation	0.211	Skewness	0.0338

Normal GOF Test		Shapiro Wilk GOF Test	
Shapiro Wilk Test Statistic	0.982	Data appear Normal at 5% Significance Level	
5% Shapiro Wilk P Value	0.677	Lilliefors GOF Test	
Lilliefors Test Statistic	0.0658	Data appear Normal at 5% Significance Level	
5% Lilliefors Critical Value	0.0968		

Data appear Normal at 5% Significance Level

Assuming Normal Distribution			
95% Normal UCL		95% UCLs (Adjusted for Skewness)	
95% Student's-t UCL	1.989	95% Adjusted-CLT UCL (Chen-1995)	1.988
		95% Modified-t UCL (Johnson-1978)	1.989

Gamma GOF Test		Anderson-Darling Gamma GOF Test	
A-D Test Statistic	0.652	Detected data appear Gamma Distributed at 5% Significance Level	
5% A-D Critical Value	0.75	Kolmogorov-Smirnov Gamma GOF Test	
K-S Test Statistic	0.0947	Detected data appear Gamma Distributed at 5% Significance Level	
5% K-S Critical Value	0.0972		

Detected data appear Gamma Distributed at 5% Significance Level

Gamma Statistics			
k hat (MLE)	21.49	k star (bias corrected MLE)	20.73
Theta hat (MLE)	0.0892	Theta star (bias corrected MLE)	0.0924
nu hat (MLE)	3610	nu star (bias corrected)	3482
MLE Mean (bias corrected)	1.916	MLE Sd (bias corrected)	0.421
Adjusted Level of Significance	0.0471	Approximate Chi Square Value (0.05)	3346
		Adjusted Chi Square Value	3344

Assuming Gamma Distribution			
95% Approximate Gamma UCL (use when n>=50))	1.994	95% Adjusted Gamma UCL (use when n<50)	1.995

Lognormal GOF Test		Shapiro Wilk Lognormal GOF Test	
Shapiro Wilk Test Statistic	0.966	Data appear Lognormal at 5% Significance Level	
5% Shapiro Wilk P Value	0.11	Lilliefors Lognormal GOF Test	
Lilliefors Test Statistic	0.108	Data Not Lognormal at 5% Significance Level	
5% Lilliefors Critical Value	0.0968		

Data appear Approximate Lognormal at 5% Significance Level

Lognormal Statistics			
Minimum of Logged Data	-0.0555	Mean of logged Data	0.627
Maximum of Logged Data	1.078	SD of logged Data	0.222

Assuming Lognormal Distribution			
95% H-UCL	2	90% Chebyshev (MVUE) UCL	2.059
95% Chebyshev (MVUE) UCL	2.123	97.5% Chebyshev (MVUE) UCL	2.212
99% Chebyshev (MVUE) UCL	2.386		

**Nonparametric Distribution Free UCL Statistics**

Data appear to follow a Discernible Distribution at 5% Significance Level

**Nonparametric Distribution Free UCLs**

95% CLT UCL	1.988	95% Jackknife UCL	1.989
95% Standard Bootstrap UCL	1.988	95% Bootstrap-t UCL	1.988
95% Hall's Bootstrap UCL	1.989	95% Percentile Bootstrap UCL	1.988
95% BCA Bootstrap UCL	1.989		
90% Chebyshev(Mean, Sd) UCL	2.048	95% Chebyshev(Mean, Sd) UCL	2.108
97.5% Chebyshev(Mean, Sd) UCL	2.191	99% Chebyshev(Mean, Sd) UCL	2.355

**Suggested UCL to Use**

95% Student's-t UCL 1.989

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL.

Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006).

However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (brc/timet\_thorium-228)

**General Statistics**

Total Number of Observations	120	Number of Distinct Observations	76
		Number of Missing Observations	0
Minimum	1.07	Mean	1.687
Maximum	2.28	Median	1.705
SD	0.278	Std. Error of Mean	0.0253
Coefficient of Variation	0.165	Skewness	-0.136

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.96
5% Shapiro Wilk P Value	0.0107
Lilliefors Test Statistic	0.0762
5% Lilliefors Critical Value	0.0812

**Shapiro Wilk GOF Test**

Data Not Normal at 5% Significance Level

**Lilliefors GOF Test**

Data appear Normal at 5% Significance Level

Data appear Approximate Normal at 5% Significance Level

**Assuming Normal Distribution**

**95% Normal UCL**

95% Student's-t UCL 1.729

**95% UCLs (Adjusted for Skewness)**

95% Adjusted-CLT UCL (Chen-1995)	1.728
95% Modified-t UCL (Johnson-1978)	1.729

**Gamma GOF Test**

A-D Test Statistic	1.132
5% A-D Critical Value	0.75
K-S Test Statistic	0.0899
5% K-S Critical Value	0.0841

**Anderson-Darling Gamma GOF Test**

Data Not Gamma Distributed at 5% Significance Level

**Kolmogorov-Smirnov Gamma GOF Test**

Data Not Gamma Distributed at 5% Significance Level

Data Not Gamma Distributed at 5% Significance Level

**Gamma Statistics**

k hat (MLE)	35.8	k star (bias corrected MLE)	34.91
Theta hat (MLE)	0.0471	Theta star (bias corrected MLE)	0.0483
nu hat (MLE)	8591	nu star (bias corrected)	8378
MLE Mean (bias corrected)	1.687	MLE Sd (bias corrected)	0.285
		Approximate Chi Square Value (0.05)	8166
Adjusted Level of Significance	0.048	Adjusted Chi Square Value	8164

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50))	1.73	95% Adjusted Gamma UCL (use when n<50)	1.731
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**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.951
5% Shapiro Wilk P Value	9.1661E-4
Lilliefors Test Statistic	0.0966
5% Lilliefors Critical Value	0.0812

**Shapiro Wilk Lognormal GOF Test**

Data Not Lognormal at 5% Significance Level

**Lilliefors Lognormal GOF Test**

Data Not Lognormal at 5% Significance Level

Data Not Lognormal at 5% Significance Level

**Lognormal Statistics**

Minimum of Logged Data	0.0677	Mean of logged Data	0.509
Maximum of Logged Data	0.824	SD of logged Data	0.17

**Assuming Lognormal Distribution**

95% H-UCL	1.733	90% Chebyshev (MVUE) UCL	1.767
95% Chebyshev (MVUE) UCL	1.802	97.5% Chebyshev (MVUE) UCL	1.852

99% Chebyshev (MVUE) UCL 1.95

**Nonparametric Distribution Free UCL Statistics**

**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**

95% CLT UCL	1.728	95% Jackknife UCL	1.729
95% Standard Bootstrap UCL	1.728	95% Bootstrap-t UCL	1.728
95% Hall's Bootstrap UCL	1.728	95% Percentile Bootstrap UCL	1.728
95% BCA Bootstrap UCL	1.728		
90% Chebyshev(Mean, Sd) UCL	1.763	95% Chebyshev(Mean, Sd) UCL	1.797
97.5% Chebyshev(Mean, Sd) UCL	1.845	99% Chebyshev(Mean, Sd) UCL	1.939

**Suggested UCL to Use**

95% Student's-t UCL 1.729

When a data set follows an approximate (e.g., normal) distribution passing one of the GOF test

When applicable, it is suggested to use a UCL based upon a distribution (e.g., gamma) passing both GOF tests in ProUCL

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

**Note: For highly negatively-skewed data, confidence limits (e.g., Chen, Johnson, Lognormal, and Gamma) may not be reliable. Chen's and Johnson's methods provide adjustments for positively skewed data sets.**

final\_numeric (brc/timet\_thorium-230)

**General Statistics**

Total Number of Observations	120	Number of Distinct Observations	82
		Number of Missing Observations	0
Minimum	0.66	Mean	1.246
Maximum	3.01	Median	1.19
SD	0.383	Std. Error of Mean	0.0349
Coefficient of Variation	0.307	Skewness	1.606

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.89	<b>Shapiro Wilk GOF Test</b>
5% Shapiro Wilk P Value	1.103E-12	Data Not Normal at 5% Significance Level
Lilliefors Test Statistic	0.131	<b>Lilliefors GOF Test</b>
5% Lilliefors Critical Value	0.0812	Data Not Normal at 5% Significance Level

**Data Not Normal at 5% Significance Level**

**Assuming Normal Distribution**

<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.304	95% Adjusted-CLT UCL (Chen-1995)	1.309
		95% Modified-t UCL (Johnson-1978)	1.305

**Gamma GOF Test**

A-D Test Statistic	1.051	<b>Anderson-Darling Gamma GOF Test</b>
5% A-D Critical Value	0.751	Data Not Gamma Distributed at 5% Significance Level
K-S Test Statistic	0.0944	<b>Kolmogorov-Smirnov Gamma GOF Test</b>
5% K-S Critical Value	0.0842	Data Not Gamma Distributed at 5% Significance Level

**Data Not Gamma Distributed at 5% Significance Level**

**Gamma Statistics**

k hat (MLE)	12.57	k star (bias corrected MLE)	12.27
Theta hat (MLE)	0.0991	Theta star (bias corrected MLE)	0.102
nu hat (MLE)	3018	nu star (bias corrected)	2944
MLE Mean (bias corrected)	1.246	MLE Sd (bias corrected)	0.356
		Approximate Chi Square Value (0.05)	2819
Adjusted Level of Significance	0.048	Adjusted Chi Square Value	2817

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50))	1.301	95% Adjusted Gamma UCL (use when n<50)	1.302
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**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.974	<b>Shapiro Wilk Lognormal GOF Test</b>
5% Shapiro Wilk P Value	0.207	Data appear Lognormal at 5% Significance Level
Lilliefors Test Statistic	0.0743	<b>Lilliefors Lognormal GOF Test</b>

5% Lilliefors Critical Value 0.0812 Data appear Lognormal at 5% Significance Level  
**Data appear Lognormal at 5% Significance Level**

**Lognormal Statistics**  
 Minimum of Logged Data -0.416 Mean of logged Data 0.18  
 Maximum of Logged Data 1.102 SD of logged Data 0.278

**Assuming Lognormal Distribution**  
 95% H-UCL 1.3 90% Chebyshev (MVUE) UCL 1.34  
 95% Chebyshev (MVUE) UCL 1.383 97.5% Chebyshev (MVUE) UCL 1.444  
 99% Chebyshev (MVUE) UCL 1.563

**Nonparametric Distribution Free UCL Statistics**  
**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**  
 95% CLT UCL 1.304 95% Jackknife UCL 1.304  
 95% Standard Bootstrap UCL 1.303 95% Bootstrap-t UCL 1.311  
 95% Hall's Bootstrap UCL 1.311 95% Percentile Bootstrap UCL 1.306  
 95% BCA Bootstrap UCL 1.307  
 90% Chebyshev(Mean, Sd) UCL 1.351 95% Chebyshev(Mean, Sd) UCL 1.398  
 97.5% Chebyshev(Mean, Sd) UCL 1.464 99% Chebyshev(Mean, Sd) UCL 1.594

**Suggested UCL to Use**  
 95% Student's-t UCL 1.304 or 95% Modified-t UCL 1.305  
 or 95% H-UCL 1.3

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL.  
 Recommendations are based upon data size, data distribution, and skewness.  
 These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006).  
 However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

**ProUCL computes and outputs H-statistic based UCLs for historical reasons only.**  
**H-statistic often results in unstable (both high and low) values of UCL95 as shown in examples in the Technical Guide.**  
**It is therefore recommended to avoid the use of H-statistic based 95% UCLs.**  
**Use of nonparametric methods are preferred to compute UCL95 for skewed data sets which do not follow a gamma distribution.**

final\_numeric (brc/timet\_thorium-232)

**General Statistics**  
 Total Number of Observations 120 Number of Distinct Observations 73  
 Number of Missing Observations 0  
 Minimum 1.05 Mean 1.614  
 Maximum 2.23 Median 1.57  
 SD 0.266 Std. Error of Mean 0.0243  
 Coefficient of Variation 0.165 Skewness 0.178

**Normal GOF Test**  
 Shapiro Wilk Test Statistic 0.961  
 5% Shapiro Wilk P Value 0.0129 Data Not Normal at 5% Significance Level  
 Lilliefors Test Statistic 0.0827 **Lilliefors GOF Test**  
 5% Lilliefors Critical Value 0.0812 Data Not Normal at 5% Significance Level  
**Data Not Normal at 5% Significance Level**

**Assuming Normal Distribution**  
**95% Normal UCL** **95% UCLs (Adjusted for Skewness)**  
 95% Student's-t UCL 1.654 95% Adjusted-CLT UCL (Chen-1995) 1.655  
 95% Modified-t UCL (Johnson-1978) 1.655

**Gamma GOF Test**  
 A-D Test Statistic 0.773 **Anderson-Darling Gamma GOF Test**  
 5% A-D Critical Value 0.75 Data Not Gamma Distributed at 5% Significance Level  
 K-S Test Statistic 0.0752 **Kolmogorov-Smirnov Gamma GOF Test**  
 5% K-S Critical Value 0.0841 Detected data appear Gamma Distributed at 5% Significance Level  
**Detected data follow Appr. Gamma Distribution at 5% Significance Level**

**Gamma Statistics**  
 k hat (MLE) 37.02 k star (bias corrected MLE) 36.1  
 Theta hat (MLE) 0.0436 Theta star (bias corrected MLE) 0.0447  
 nu hat (MLE) 8885 nu star (bias corrected) 8664  
 MLE Mean (bias corrected) 1.614 MLE Sd (bias corrected) 0.269

Adjusted Level of Significance	0.048	Approximate Chi Square Value (0.05)	8449
		Adjusted Chi Square Value	8446

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50)	1.655	95% Adjusted Gamma UCL (use when n<50)	1.656
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**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.965
5% Shapiro Wilk P Value	0.0349
Lilliefors Test Statistic	0.0794
5% Lilliefors Critical Value	0.0812

**Shapiro Wilk Lognormal GOF Test**

Data Not Lognormal at 5% Significance Level

**Lilliefors Lognormal GOF Test**

Data appear Lognormal at 5% Significance Level

**Data appear Approximate Lognormal at 5% Significance Level**

**Lognormal Statistics**

Minimum of Logged Data	0.0488	Mean of logged Data	0.465
Maximum of Logged Data	0.802	SD of logged Data	0.166

**Assuming Lognormal Distribution**

95% H-UCL	1.657	90% Chebyshev (MVUE) UCL	1.688
95% Chebyshev (MVUE) UCL	1.722	97.5% Chebyshev (MVUE) UCL	1.768
99% Chebyshev (MVUE) UCL	1.859		

**Nonparametric Distribution Free UCL Statistics**

**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**

95% CLT UCL	1.654	95% Jackknife UCL	1.654
95% Standard Bootstrap UCL	1.654	95% Bootstrap-t UCL	1.655
95% Hall's Bootstrap UCL	1.655	95% Percentile Bootstrap UCL	1.654
95% BCA Bootstrap UCL	1.653		
90% Chebyshev(Mean, Sd) UCL	1.687	95% Chebyshev(Mean, Sd) UCL	1.72
97.5% Chebyshev(Mean, Sd) UCL	1.766	99% Chebyshev(Mean, Sd) UCL	1.856

**Suggested UCL to Use**

95% Approximate Gamma UCL 1.655

When a data set follows an approximate (e.g., normal) distribution passing one of the GOF test

When applicable, it is suggested to use a UCL based upon a distribution (e.g., gamma) passing both GOF tests in ProUCL

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL.

Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006).

However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (brc/timet\_uranium-234)

**General Statistics**

Total Number of Observations	120	Number of Distinct Observations	74
		Number of Missing Observations	0
Minimum	0.47	Mean	1.109
Maximum	2.84	Median	0.99
SD	0.457	Std. Error of Mean	0.0417
Coefficient of Variation	0.412	Skewness	1.792

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.819
5% Shapiro Wilk P Value	0
Lilliefors Test Statistic	0.195
5% Lilliefors Critical Value	0.0812

**Shapiro Wilk GOF Test**

Data Not Normal at 5% Significance Level

**Lilliefors GOF Test**

Data Not Normal at 5% Significance Level

**Data Not Normal at 5% Significance Level**

**Assuming Normal Distribution**

95% Normal UCL		95% UCLs (Adjusted for Skewness)	
95% Student's-t UCL	1.178	95% Adjusted-CLT UCL (Chen-1995)	1.185
		95% Modified-t UCL (Johnson-1978)	1.179

**Gamma GOF Test**

A-D Test Statistic	3.149
5% A-D Critical Value	0.753
K-S Test Statistic	0.14
5% K-S Critical Value	0.0843

**Anderson-Darling Gamma GOF Test**

Data Not Gamma Distributed at 5% Significance Level

**Kolmogorov-Smirnov Gamma GOF Test**

Data Not Gamma Distributed at 5% Significance Level

**Data Not Gamma Distributed at 5% Significance Level**

<b>Gamma Statistics</b>			
k hat (MLE)	7.606	k star (bias corrected MLE)	7.422
Theta hat (MLE)	0.146	Theta star (bias corrected MLE)	0.149
nu hat (MLE)	1825	nu star (bias corrected)	1781
MLE Mean (bias corrected)	1.109	MLE Sd (bias corrected)	0.407
		Approximate Chi Square Value (0.05)	1684
Adjusted Level of Significance	0.048	Adjusted Chi Square Value	1683
<b>Assuming Gamma Distribution</b>			
95% Approximate Gamma UCL (use when n>=50))	1.173	95% Adjusted Gamma UCL (use when n<50)	1.174

<b>Lognormal GOF Test</b>		<b>Shapiro Wilk Lognormal GOF Test</b>	
Shapiro Wilk Test Statistic	0.947	Data Not Lognormal at 5% Significance Level	
5% Shapiro Wilk P Value	2.4870E-4	<b>Lilliefors Lognormal GOF Test</b>	
Lilliefors Test Statistic	0.115	Data Not Lognormal at 5% Significance Level	
5% Lilliefors Critical Value	0.0812		

**Data Not Lognormal at 5% Significance Level**

<b>Lognormal Statistics</b>			
Minimum of Logged Data	-0.755	Mean of logged Data	0.0362
Maximum of Logged Data	1.044	SD of logged Data	0.353
<b>Assuming Lognormal Distribution</b>			
95% H-UCL	1.168	90% Chebyshev (MVUE) UCL	1.212
95% Chebyshev (MVUE) UCL	1.262	97.5% Chebyshev (MVUE) UCL	1.331
99% Chebyshev (MVUE) UCL	1.466		

**Nonparametric Distribution Free UCL Statistics**  
**Data do not follow a Discernible Distribution (0.05)**

<b>Nonparametric Distribution Free UCLs</b>			
95% CLT UCL	1.178	95% Jackknife UCL	1.178
95% Standard Bootstrap UCL	1.177	95% Bootstrap-t UCL	1.187
95% Hall's Bootstrap UCL	1.188	95% Percentile Bootstrap UCL	1.179
95% BCA Bootstrap UCL	1.186		
90% Chebyshev(Mean, Sd) UCL	1.234	95% Chebyshev(Mean, Sd) UCL	1.291
97.5% Chebyshev(Mean, Sd) UCL	1.37	99% Chebyshev(Mean, Sd) UCL	1.524

<b>Suggested UCL to Use</b>			
95% Student's-t UCL	1.178	or 95% Modified-t UCL	1.179

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

**final\_numeric (brc/timet\_uranium-235)**

<b>General Statistics</b>			
Total Number of Observations	120	Number of Distinct Observations	76
		Number of Missing Observations	0
Minimum	0	Mean	0.0659
Maximum	0.21	Median	0.059
SD	0.0382	Std. Error of Mean	0.00349
Coefficient of Variation	0.579	Skewness	0.82
<b>Normal GOF Test</b>			
Shapiro Wilk Test Statistic	0.953	<b>Shapiro Wilk GOF Test</b>	
5% Shapiro Wilk P Value	0.00163	Data Not Normal at 5% Significance Level	
Lilliefors Test Statistic	0.109	<b>Lilliefors GOF Test</b>	
5% Lilliefors Critical Value	0.0812	Data Not Normal at 5% Significance Level	

**Data Not Normal at 5% Significance Level**

<b>Assuming Normal Distribution</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Normal UCL		95% Adjusted-CLT UCL (Chen-1995)	0.0719
95% Student's-t UCL	0.0717	95% Modified-t UCL (Johnson-1978)	0.0717

**Gamma Statistics Not Available**  
**Lognormal Statistics Not Available**



**Nonparametric Distribution Free UCL Statistics**  
**Data do not follow a Discernible Distribution (0.05)**

Nonparametric Distribution Free UCLs			
95% CLT UCL	0.0716	95% Jackknife UCL	0.0717
95% Standard Bootstrap UCL	0.0717	95% Bootstrap-t UCL	0.072
95% Hall's Bootstrap UCL	0.0719	95% Percentile Bootstrap UCL	0.0716
95% BCA Bootstrap UCL	0.0719		
90% Chebyshev(Mean, Sd) UCL	0.0764	95% Chebyshev(Mean, Sd) UCL	0.0811
97.5% Chebyshev(Mean, Sd) UCL	0.0877	99% Chebyshev(Mean, Sd) UCL	0.101
<b>Suggested UCL to Use</b>			
95% Chebyshev (Mean, Sd) UCL	0.0811		

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (brc/timet\_uranium-238)

General Statistics			
Total Number of Observations	120	Number of Distinct Observations	75
		Number of Missing Observations	0
Minimum	0.45	Mean	1.085
Maximum	2.37	Median	1.015
SD	0.373	Std. Error of Mean	0.0341
Coefficient of Variation	0.344	Skewness	1.298

Normal GOF Test		Shapiro Wilk GOF Test	
Shapiro Wilk Test Statistic	0.895	Data Not Normal at 5% Significance Level	
5% Shapiro Wilk P Value	5.103E-12	<b>Lilliefors GOF Test</b>	
Lilliefors Test Statistic	0.151	Data Not Normal at 5% Significance Level	
5% Lilliefors Critical Value	0.0812		

**Data Not Normal at 5% Significance Level**

Assuming Normal Distribution			
<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.141	95% Adjusted-CLT UCL (Chen-1995)	1.145
		95% Modified-t UCL (Johnson-1978)	1.142

Gamma GOF Test		Anderson-Darling Gamma GOF Test	
A-D Test Statistic	1.449	Data Not Gamma Distributed at 5% Significance Level	
5% A-D Critical Value	0.752	<b>Kolmogorov-Smirnov Gamma GOF Test</b>	
K-S Test Statistic	0.106	Data Not Gamma Distributed at 5% Significance Level	
5% K-S Critical Value	0.0842		

**Data Not Gamma Distributed at 5% Significance Level**

Gamma Statistics			
k hat (MLE)	9.691	k star (bias corrected MLE)	9.454
Theta hat (MLE)	0.112	Theta star (bias corrected MLE)	0.115
nu hat (MLE)	2326	nu star (bias corrected)	2269
MLE Mean (bias corrected)	1.085	MLE Sd (bias corrected)	0.353
Adjusted Level of Significance	0.048	Approximate Chi Square Value (0.05)	2159
		Adjusted Chi Square Value	2158

Assuming Gamma Distribution			
95% Approximate Gamma UCL (use when n>=50))	1.14	95% Adjusted Gamma UCL (use when n<50)	1.14

Lognormal GOF Test		Shapiro Wilk Lognormal GOF Test	
Shapiro Wilk Test Statistic	0.973	Data appear Lognormal at 5% Significance Level	
5% Shapiro Wilk P Value	0.158	<b>Lilliefors Lognormal GOF Test</b>	
Lilliefors Test Statistic	0.0861	Data Not Lognormal at 5% Significance Level	
5% Lilliefors Critical Value	0.0812		

**Data appear Approximate Lognormal at 5% Significance Level**

Lognormal Statistics			
Minimum of Logged Data	-0.799	Mean of logged Data	0.0286
Maximum of Logged Data	0.863	SD of logged Data	0.321



<b>Assuming Lognormal Distribution</b>			
95% H-UCL	1.14	90% Chebyshev (MVUE) UCL	1.18
95% Chebyshev (MVUE) UCL	1.224	97.5% Chebyshev (MVUE) UCL	1.286
99% Chebyshev (MVUE) UCL	1.406		

**Nonparametric Distribution Free UCL Statistics**  
**Data appear to follow a Discernible Distribution at 5% Significance Level**

<b>Nonparametric Distribution Free UCLs</b>			
95% CLT UCL	1.141	95% Jackknife UCL	1.141
95% Standard Bootstrap UCL	1.141	95% Bootstrap-t UCL	1.146
95% Hall's Bootstrap UCL	1.146	95% Percentile Bootstrap UCL	1.141
95% BCA Bootstrap UCL	1.144		
90% Chebyshev(Mean, Sd) UCL	1.187	95% Chebyshev(Mean, Sd) UCL	1.233
97.5% Chebyshev(Mean, Sd) UCL	1.297	99% Chebyshev(Mean, Sd) UCL	1.424

<b>Suggested UCL to Use</b>			
95% Student's-t UCL	1.141	or 95% Modified-t UCL	1.142
or 95% H-UCL	1.14		

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

**ProUCL computes and outputs H-statistic based UCLs for historical reasons only.**  
**H-statistic often results in unstable (both high and low) values of UCL95 as shown in examples in the Technical Guide.**  
**It is therefore recommended to avoid the use of H-statistic based 95% UCLs.**  
**Use of nonparametric methods are preferred to compute UCL95 for skewed data sets which do not follow a gamma distribution.**

final\_numeric (rz-a\_radium-226)

<b>General Statistics</b>			
Total Number of Observations	31	Number of Distinct Observations	29
		Number of Missing Observations	0
Minimum	0.0472	Mean	0.952
Maximum	1.72	Median	0.891
SD	0.354	Std. Error of Mean	0.0636
Coefficient of Variation	0.372	Skewness	0.101

<b>Normal GOF Test</b>		<b>Shapiro Wilk GOF Test</b>	
Shapiro Wilk Test Statistic	0.966	Data appear Normal at 5% Significance Level	
5% Shapiro Wilk Critical Value	0.929	<b>Lilliefors GOF Test</b>	
Lilliefors Test Statistic	0.114	Data appear Normal at 5% Significance Level	
5% Lilliefors Critical Value	0.156		

**Data appear Normal at 5% Significance Level**

<b>Assuming Normal Distribution</b>			
<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.06	95% Adjusted-CLT UCL (Chen-1995)	1.058
		95% Modified-t UCL (Johnson-1978)	1.06

<b>Gamma GOF Test</b>		<b>Anderson-Darling Gamma GOF Test</b>	
A-D Test Statistic	1.162	Data Not Gamma Distributed at 5% Significance Level	
5% A-D Critical Value	0.748	<b>Kolmogorov-Smirnov Gamma GOF Test</b>	
K-S Test Statistic	0.179	Data Not Gamma Distributed at 5% Significance Level	
5% K-S Critical Value	0.158		

**Data Not Gamma Distributed at 5% Significance Level**

<b>Gamma Statistics</b>			
k hat (MLE)	4.548	k star (bias corrected MLE)	4.129
Theta hat (MLE)	0.209	Theta star (bias corrected MLE)	0.231
nu hat (MLE)	282	nu star (bias corrected)	256
MLE Mean (bias corrected)	0.952	MLE Sd (bias corrected)	0.469
		Approximate Chi Square Value (0.05)	220
Adjusted Level of Significance	0.0413	Adjusted Chi Square Value	218.1

<b>Assuming Gamma Distribution</b>			
95% Approximate Gamma UCL (use when n>=50))	1.108	95% Adjusted Gamma UCL (use when n<50)	1.118

**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.669	<b>Shapiro Wilk Lognormal GOF Test</b>
5% Shapiro Wilk Critical Value	0.929	Data Not Lognormal at 5% Significance Level
Lilliefors Test Statistic	0.233	<b>Lilliefors Lognormal GOF Test</b>
5% Lilliefors Critical Value	0.156	Data Not Lognormal at 5% Significance Level

**Data Not Lognormal at 5% Significance Level**

**Lognormal Statistics**

Minimum of Logged Data	-3.053	Mean of logged Data	-0.163
Maximum of Logged Data	0.542	SD of logged Data	0.62

**Assuming Lognormal Distribution**

95% H-UCL	1.296	90% Chebyshev (MVUE) UCL	1.387
95% Chebyshev (MVUE) UCL	1.552	97.5% Chebyshev (MVUE) UCL	1.781
99% Chebyshev (MVUE) UCL	2.231		

**Nonparametric Distribution Free UCL Statistics**

**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**

95% CLT UCL	1.057	95% Jackknife UCL	1.06
95% Standard Bootstrap UCL	1.056	95% Bootstrap-t UCL	1.063
95% Hall's Bootstrap UCL	1.061	95% Percentile Bootstrap UCL	1.057
95% BCA Bootstrap UCL	1.06		
90% Chebyshev(Mean, Sd) UCL	1.143	95% Chebyshev(Mean, Sd) UCL	1.23
97.5% Chebyshev(Mean, Sd) UCL	1.35	99% Chebyshev(Mean, Sd) UCL	1.585

**Suggested UCL to Use**

95% Student's-t UCL 1.06

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (rz-a\_radium-228)

**General Statistics**

Total Number of Observations	31	Number of Distinct Observations	30
		Number of Missing Observations	0
Minimum	0.46	Mean	1.279
Maximum	2.46	Median	1.18
SD	0.542	Std. Error of Mean	0.0974
Coefficient of Variation	0.424	Skewness	0.51

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.957	<b>Shapiro Wilk GOF Test</b>
5% Shapiro Wilk Critical Value	0.929	Data appear Normal at 5% Significance Level
Lilliefors Test Statistic	0.0888	<b>Lilliefors GOF Test</b>
5% Lilliefors Critical Value	0.156	Data appear Normal at 5% Significance Level

**Data appear Normal at 5% Significance Level**

**Assuming Normal Distribution**

<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.445	95% Adjusted-CLT UCL (Chen-1995)	1.449
		95% Modified-t UCL (Johnson-1978)	1.446

**Gamma GOF Test**

A-D Test Statistic	0.13	<b>Anderson-Darling Gamma GOF Test</b>
5% A-D Critical Value	0.747	Detected data appear Gamma Distributed at 5% Significance Level
K-S Test Statistic	0.0688	<b>Kolmogorov-Smirnov Gamma GOF Test</b>
5% K-S Critical Value	0.158	Detected data appear Gamma Distributed at 5% Significance Level

**Detected data appear Gamma Distributed at 5% Significance Level**

**Gamma Statistics**

k hat (MLE)	5.597	k star (bias corrected MLE)	5.076
Theta hat (MLE)	0.229	Theta star (bias corrected MLE)	0.252
nu hat (MLE)	347	nu star (bias corrected)	314.7
MLE Mean (bias corrected)	1.279	MLE Sd (bias corrected)	0.568
		Approximate Chi Square Value (0.05)	274.6
Adjusted Level of Significance	0.0413	Adjusted Chi Square Value	272.6

**Assuming Gamma Distribution**  
 95% Approximate Gamma UCL (use when n>=50) 1.466 95% Adjusted Gamma UCL (use when n<50) 1.477

**Lognormal GOF Test**  
 Shapiro Wilk Test Statistic 0.974 **Shapiro Wilk Lognormal GOF Test**  
 5% Shapiro Wilk Critical Value 0.929 Data appear Lognormal at 5% Significance Level  
 Lilliefors Test Statistic 0.0712 **Lilliefors Lognormal GOF Test**  
 5% Lilliefors Critical Value 0.156 Data appear Lognormal at 5% Significance Level  
**Data appear Lognormal at 5% Significance Level**

**Lognormal Statistics**  
 Minimum of Logged Data -0.777 Mean of logged Data 0.154  
 Maximum of Logged Data 0.9 SD of logged Data 0.447

**Assuming Lognormal Distribution**  
 95% H-UCL 1.504 90% Chebyshev (MVUE) UCL 1.606  
 95% Chebyshev (MVUE) UCL 1.751 97.5% Chebyshev (MVUE) UCL 1.952  
 99% Chebyshev (MVUE) UCL 2.348

**Nonparametric Distribution Free UCL Statistics**  
**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**  
 95% CLT UCL 1.44 95% Jackknife UCL 1.445  
 95% Standard Bootstrap UCL 1.438 95% Bootstrap-t UCL 1.453  
 95% Hall's Bootstrap UCL 1.446 95% Percentile Bootstrap UCL 1.444  
 95% BCA Bootstrap UCL 1.444  
 90% Chebyshev(Mean, Sd) UCL 1.572 95% Chebyshev(Mean, Sd) UCL 1.704  
 97.5% Chebyshev(Mean, Sd) UCL 1.888 99% Chebyshev(Mean, Sd) UCL 2.248

**Suggested UCL to Use**  
 95% Student's-t UCL 1.445

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness. These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (rz-a\_thorium-228)

**General Statistics**  
 Total Number of Observations 31 Number of Distinct Observations 30  
 Number of Missing Observations 0  
 Minimum 1.16 Mean 1.696  
 Maximum 2.88 Median 1.69  
 SD 0.361 Std. Error of Mean 0.0648  
 Coefficient of Variation 0.213 Skewness 1.023

**Normal GOF Test**  
 Shapiro Wilk Test Statistic 0.929 **Shapiro Wilk GOF Test**  
 5% Shapiro Wilk Critical Value 0.929 Data Not Normal at 5% Significance Level  
 Lilliefors Test Statistic 0.0999 **Lilliefors GOF Test**  
 5% Lilliefors Critical Value 0.156 Data appear Normal at 5% Significance Level  
**Data appear Approximate Normal at 5% Significance Level**

**Assuming Normal Distribution**  
**95% Normal UCL** **95% UCLs (Adjusted for Skewness)**  
 95% Student's-t UCL 1.806 95% Adjusted-CLT UCL (Chen-1995) 1.816  
 95% Modified-t UCL (Johnson-1978) 1.808

**Gamma GOF Test**  
 A-D Test Statistic 0.324 **Anderson-Darling Gamma GOF Test**  
 5% A-D Critical Value 0.745 Detected data appear Gamma Distributed at 5% Significance Level  
 K-S Test Statistic 0.0823 **Kolmogorov-Smirnov Gamma GOF Test**  
 5% K-S Critical Value 0.157 Detected data appear Gamma Distributed at 5% Significance Level  
**Detected data appear Gamma Distributed at 5% Significance Level**

**Gamma Statistics**  
 k hat (MLE) 24.47 k star (bias corrected MLE) 22.12  
 Theta hat (MLE) 0.0693 Theta star (bias corrected MLE) 0.0767  
 nu hat (MLE) 1517 nu star (bias corrected) 1372

MLE Mean (bias corrected)	1.696	MLE Sd (bias corrected)	0.361
Adjusted Level of Significance	0.0413	Approximate Chi Square Value (0.05)	1287
		Adjusted Chi Square Value	1282

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50))	1.809	95% Adjusted Gamma UCL (use when n<50)	1.815
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**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.968	<b>Shapiro Wilk Lognormal GOF Test</b>
5% Shapiro Wilk Critical Value	0.929	Data appear Lognormal at 5% Significance Level
Lilliefors Test Statistic	0.0781	<b>Lilliefors Lognormal GOF Test</b>
5% Lilliefors Critical Value	0.156	Data appear Lognormal at 5% Significance Level

Data appear Lognormal at 5% Significance Level

**Lognormal Statistics**

Minimum of Logged Data	0.148	Mean of logged Data	0.508
Maximum of Logged Data	1.058	SD of logged Data	0.204

**Assuming Lognormal Distribution**

95% H-UCL	1.811	90% Chebyshev (MVUE) UCL	1.884
95% Chebyshev (MVUE) UCL	1.969	97.5% Chebyshev (MVUE) UCL	2.087
99% Chebyshev (MVUE) UCL	2.319		

**Nonparametric Distribution Free UCL Statistics**

Data appear to follow a Discernible Distribution at 5% Significance Level

**Nonparametric Distribution Free UCLs**

95% CLT UCL	1.803	95% Jackknife UCL	1.806
95% Standard Bootstrap UCL	1.801	95% Bootstrap-t UCL	1.821
95% Hall's Bootstrap UCL	1.836	95% Percentile Bootstrap UCL	1.802
95% BCA Bootstrap UCL	1.813		
90% Chebyshev(Mean, Sd) UCL	1.891	95% Chebyshev(Mean, Sd) UCL	1.979
97.5% Chebyshev(Mean, Sd) UCL	2.101	99% Chebyshev(Mean, Sd) UCL	2.341

**Suggested UCL to Use**

95% Student's-t UCL 1.806

When a data set follows an approximate (e.g., normal) distribution passing one of the GOF test  
When applicable, it is suggested to use a UCL based upon a distribution (e.g., gamma) passing both GOF tests in ProUCL

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL.  
Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006).  
However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (rz-a\_thorium-230)

**General Statistics**

Total Number of Observations	31	Number of Distinct Observations	29
		Number of Missing Observations	0
Minimum	0.509	Mean	1.079
Maximum	1.71	Median	1.07
SD	0.283	Std. Error of Mean	0.0507
Coefficient of Variation	0.262	Skewness	0.392

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.975	<b>Shapiro Wilk GOF Test</b>
5% Shapiro Wilk Critical Value	0.929	Data appear Normal at 5% Significance Level
Lilliefors Test Statistic	0.111	<b>Lilliefors GOF Test</b>
5% Lilliefors Critical Value	0.156	Data appear Normal at 5% Significance Level

Data appear Normal at 5% Significance Level

**Assuming Normal Distribution**

<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.165	95% Adjusted-CLT UCL (Chen-1995)	1.166
		95% Modified-t UCL (Johnson-1978)	1.166

**Gamma GOF Test**

A-D Test Statistic	0.186	<b>Anderson-Darling Gamma GOF Test</b>
5% A-D Critical Value	0.745	Detected data appear Gamma Distributed at 5% Significance Level
K-S Test Statistic	0.0809	<b>Kolmogorov-Smirnov Gamma GOF Test</b>

5% K-S Critical Value 0.158 Detected data appear Gamma Distributed at 5% Significance Level  
**Detected data appear Gamma Distributed at 5% Significance Level**

<b>Gamma Statistics</b>			
k hat (MLE)	14.73	k star (bias corrected MLE)	13.32
Theta hat (MLE)	0.0733	Theta star (bias corrected MLE)	0.081
nu hat (MLE)	913.1	nu star (bias corrected)	826.1
MLE Mean (bias corrected)	1.079	MLE Sd (bias corrected)	0.296
		Approximate Chi Square Value (0.05)	760.4
Adjusted Level of Significance	0.0413	Adjusted Chi Square Value	756.9

**Assuming Gamma Distribution**  
 95% Approximate Gamma UCL (use when n>=50)) 1.172 95% Adjusted Gamma UCL (use when n<50) 1.178

<b>Lognormal GOF Test</b>		<b>Shapiro Wilk Lognormal GOF Test</b>	
Shapiro Wilk Test Statistic	0.977	Data appear Lognormal at 5% Significance Level	
5% Shapiro Wilk Critical Value	0.929	<b>Lilliefors Lognormal GOF Test</b>	
Lilliefors Test Statistic	0.0776	Data appear Lognormal at 5% Significance Level	
5% Lilliefors Critical Value	0.156	<b>Data appear Lognormal at 5% Significance Level</b>	

<b>Lognormal Statistics</b>			
Minimum of Logged Data	-0.675	Mean of logged Data	0.0418
Maximum of Logged Data	0.536	SD of logged Data	0.271

**Assuming Lognormal Distribution**  
 95% H-UCL 1.181 90% Chebyshev (MVUE) UCL 1.24  
 95% Chebyshev (MVUE) UCL 1.313 97.5% Chebyshev (MVUE) UCL 1.413  
 99% Chebyshev (MVUE) UCL 1.611

**Nonparametric Distribution Free UCL Statistics**  
**Data appear to follow a Discernible Distribution at 5% Significance Level**

<b>Nonparametric Distribution Free UCLs</b>			
95% CLT UCL	1.163	95% Jackknife UCL	1.165
95% Standard Bootstrap UCL	1.161	95% Bootstrap-t UCL	1.171
95% Hall's Bootstrap UCL	1.171	95% Percentile Bootstrap UCL	1.161
95% BCA Bootstrap UCL	1.165		
90% Chebyshev(Mean, Sd) UCL	1.231	95% Chebyshev(Mean, Sd) UCL	1.3
97.5% Chebyshev(Mean, Sd) UCL	1.396	99% Chebyshev(Mean, Sd) UCL	1.584

**Suggested UCL to Use**  
 95% Student's-t UCL 1.165

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness. These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (rz-a\_thorium-232)

<b>General Statistics</b>			
Total Number of Observations	31	Number of Distinct Observations	28
		Number of Missing Observations	0
Minimum	1.02	Mean	1.503
Maximum	2.07	Median	1.51
SD	0.238	Std. Error of Mean	0.0428
Coefficient of Variation	0.159	Skewness	0.137

<b>Normal GOF Test</b>		<b>Shapiro Wilk GOF Test</b>	
Shapiro Wilk Test Statistic	0.99	Data appear Normal at 5% Significance Level	
5% Shapiro Wilk Critical Value	0.929	<b>Lilliefors GOF Test</b>	
Lilliefors Test Statistic	0.059	Data appear Normal at 5% Significance Level	
5% Lilliefors Critical Value	0.156	<b>Data appear Normal at 5% Significance Level</b>	

**Assuming Normal Distribution**  
 95% Normal UCL 95% UCLs (Adjusted for Skewness)  
 95% Student's-t UCL 1.576 95% Adjusted-CLT UCL (Chen-1995) 1.574  
 95% Modified-t UCL (Johnson-1978) 1.576

<b>Gamma GOF Test</b>			<b>Anderson-Darling Gamma GOF Test</b>		
A-D Test Statistic	0.161		Detected data appear Gamma Distributed at 5% Significance Level		
5% A-D Critical Value	0.744				
K-S Test Statistic	0.0797		<b>Kolmogorov-Smirnov Gamma GOF Test</b>		
5% K-S Critical Value	0.157		Detected data appear Gamma Distributed at 5% Significance Level		
<b>Detected data appear Gamma Distributed at 5% Significance Level</b>					

<b>Gamma Statistics</b>					
k hat (MLE)	40.43		k star (bias corrected MLE)	36.54	
Theta hat (MLE)	0.0372		Theta star (bias corrected MLE)	0.0411	
nu hat (MLE)	2507		nu star (bias corrected)	2265	
MLE Mean (bias corrected)	1.503		MLE Sd (bias corrected)	0.249	
			Approximate Chi Square Value (0.05)	2156	
Adjusted Level of Significance	0.0413		Adjusted Chi Square Value	2150	

<b>Assuming Gamma Distribution</b>			
95% Approximate Gamma UCL (use when n>=50))	1.579	95% Adjusted Gamma UCL (use when n<50)	1.584

<b>Lognormal GOF Test</b>			<b>Shapiro Wilk Lognormal GOF Test</b>		
Shapiro Wilk Test Statistic	0.985		Data appear Lognormal at 5% Significance Level		
5% Shapiro Wilk Critical Value	0.929				
Lilliefors Test Statistic	0.09		<b>Lilliefors Lognormal GOF Test</b>		
5% Lilliefors Critical Value	0.156		Data appear Lognormal at 5% Significance Level		
<b>Data appear Lognormal at 5% Significance Level</b>					

<b>Lognormal Statistics</b>					
Minimum of Logged Data	0.0198		Mean of logged Data	0.395	
Maximum of Logged Data	0.728		SD of logged Data	0.161	

<b>Assuming Lognormal Distribution</b>			
95% H-UCL	1.582	90% Chebyshev (MVUE) UCL	1.635
95% Chebyshev (MVUE) UCL	1.694	97.5% Chebyshev (MVUE) UCL	1.777
99% Chebyshev (MVUE) UCL	1.939		

**Nonparametric Distribution Free UCL Statistics**  
**Data appear to follow a Discernible Distribution at 5% Significance Level**

<b>Nonparametric Distribution Free UCLs</b>			
95% CLT UCL	1.573	95% Jackknife UCL	1.576
95% Standard Bootstrap UCL	1.572	95% Bootstrap-t UCL	1.576
95% Hall's Bootstrap UCL	1.576	95% Percentile Bootstrap UCL	1.572
95% BCA Bootstrap UCL	1.575		
90% Chebyshev(Mean, Sd) UCL	1.631	95% Chebyshev(Mean, Sd) UCL	1.689
97.5% Chebyshev(Mean, Sd) UCL	1.77	99% Chebyshev(Mean, Sd) UCL	1.929

**Suggested UCL to Use**  
**95% Student's-t UCL 1.576**

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (rz-a\_uranium-234)

<b>General Statistics</b>			
Total Number of Observations	31	Number of Distinct Observations	27
		Number of Missing Observations	0
Minimum	0.391	Mean	1.062
Maximum	1.74	Median	1.02
SD	0.297	Std. Error of Mean	0.0534
Coefficient of Variation	0.28	Skewness	0.571

<b>Normal GOF Test</b>			<b>Shapiro Wilk GOF Test</b>		
Shapiro Wilk Test Statistic	0.942		Data appear Normal at 5% Significance Level		
5% Shapiro Wilk Critical Value	0.929				
Lilliefors Test Statistic	0.135		<b>Lilliefors GOF Test</b>		
5% Lilliefors Critical Value	0.156		Data appear Normal at 5% Significance Level		
<b>Data appear Normal at 5% Significance Level</b>					

**Assuming Normal Distribution**

<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.153	95% Adjusted-CLT UCL (Chen-1995)	1.156
		95% Modified-t UCL (Johnson-1978)	1.154

**Gamma GOF Test**

A-D Test Statistic	0.518
5% A-D Critical Value	0.746
K-S Test Statistic	0.102
5% K-S Critical Value	0.158

Anderson-Darling Gamma GOF Test  
Detected data appear Gamma Distributed at 5% Significance Level

**Kolmogorov-Smirnov Gamma GOF Test**

Detected data appear Gamma Distributed at 5% Significance Level

**Detected data appear Gamma Distributed at 5% Significance Level**

**Gamma Statistics**

k hat (MLE)	12.85
Theta hat (MLE)	0.0827
nu hat (MLE)	796.5
MLE Mean (bias corrected)	1.062
Adjusted Level of Significance	0.0413

k star (bias corrected MLE)	11.62
Theta star (bias corrected MLE)	0.0914
nu star (bias corrected)	720.7
MLE Sd (bias corrected)	0.312
Approximate Chi Square Value (0.05)	659.4
Adjusted Chi Square Value	656.2

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50))	1.161	95% Adjusted Gamma UCL (use when n<50)	1.167
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**Lognormal GOF Test**

Shapiro Wilk Test Statistic	0.933
5% Shapiro Wilk Critical Value	0.929
Lilliefors Test Statistic	0.114
5% Lilliefors Critical Value	0.156

Shapiro Wilk Lognormal GOF Test  
Data appear Lognormal at 5% Significance Level

**Lilliefors Lognormal GOF Test**

Data appear Lognormal at 5% Significance Level

**Data appear Lognormal at 5% Significance Level**

**Lognormal Statistics**

Minimum of Logged Data	-0.939
Maximum of Logged Data	0.554

Mean of logged Data	0.0212
SD of logged Data	0.293

**Assuming Lognormal Distribution**

95% H-UCL	1.174
95% Chebyshev (MVUE) UCL	1.313
99% Chebyshev (MVUE) UCL	1.632

90% Chebyshev (MVUE) UCL	1.236
97.5% Chebyshev (MVUE) UCL	1.421

**Nonparametric Distribution Free UCL Statistics**

**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**

95% CLT UCL	1.15
95% Standard Bootstrap UCL	1.149
95% Hall's Bootstrap UCL	1.161
95% BCA Bootstrap UCL	1.154
90% Chebyshev(Mean, Sd) UCL	1.223
97.5% Chebyshev(Mean, Sd) UCL	1.396

95% Jackknife UCL	1.153
95% Bootstrap-t UCL	1.161
95% Percentile Bootstrap UCL	1.15
95% Chebyshev(Mean, Sd) UCL	1.295
99% Chebyshev(Mean, Sd) UCL	1.594

**Suggested UCL to Use**

95% Student's-t UCL	1.153
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Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness.

These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (rz-a\_uranium-235)

**General Statistics**

Total Number of Observations	31
Minimum	-0.0766
Maximum	0.203
SD	0.0442
Coefficient of Variation	0.862

Number of Distinct Observations	29
Number of Missing Observations	0
Mean	0.0513
Median	0.0486
Std. Error of Mean	0.00794
Skewness	0.549

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.892
5% Shapiro Wilk Critical Value	0.929
Lilliefors Test Statistic	0.132

**Shapiro Wilk GOF Test**

Data Not Normal at 5% Significance Level

**Lilliefors GOF Test**



5% Lilliefors Critical Value 0.156 Data appear Normal at 5% Significance Level  
**Data appear Approximate Normal at 5% Significance Level**

**Assuming Normal Distribution**

<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	0.0648	95% Adjusted-CLT UCL (Chen-1995)	0.0652
		95% Modified-t UCL (Johnson-1978)	0.0649

**Gamma Statistics Not Available**  
**Lognormal Statistics Not Available**

**Nonparametric Distribution Free UCL Statistics**  
**Data appear to follow a Discernible Distribution at 5% Significance Level**

**Nonparametric Distribution Free UCLs**

95% CLT UCL	0.0644	95% Jackknife UCL	0.0648
95% Standard Bootstrap UCL	0.0642	95% Bootstrap-t UCL	0.0658
95% Hall's Bootstrap UCL	0.0689	95% Percentile Bootstrap UCL	0.0643
95% BCA Bootstrap UCL	0.0648		
90% Chebyshev(Mean, Sd) UCL	0.0751	95% Chebyshev(Mean, Sd) UCL	0.0859
97.5% Chebyshev(Mean, Sd) UCL	0.101	99% Chebyshev(Mean, Sd) UCL	0.13

**Suggested UCL to Use**  
95% Student's-t UCL 0.0648

When a data set follows an approximate (e.g., normal) distribution passing one of the GOF test  
When applicable, it is suggested to use a UCL based upon a distribution (e.g., gamma) passing both GOF tests in ProUCL

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL.  
Recommendations are based upon data size, data distribution, and skewness.  
These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006).  
However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

final\_numeric (rz-a\_uranium-238)

**General Statistics**

Total Number of Observations	31	Number of Distinct Observations	26
		Number of Missing Observations	0
Minimum	0.361	Mean	1.034
Maximum	1.59	Median	1.01
SD	0.214	Std. Error of Mean	0.0384
Coefficient of Variation	0.207	Skewness	-0.157

**Normal GOF Test**

Shapiro Wilk Test Statistic	0.898	<b>Shapiro Wilk GOF Test</b>	
5% Shapiro Wilk Critical Value	0.929	Data Not Normal at 5% Significance Level	
Lilliefors Test Statistic	0.186	<b>Lilliefors GOF Test</b>	
5% Lilliefors Critical Value	0.156	Data Not Normal at 5% Significance Level	

**Data Not Normal at 5% Significance Level**

**Assuming Normal Distribution**

<b>95% Normal UCL</b>		<b>95% UCLs (Adjusted for Skewness)</b>	
95% Student's-t UCL	1.099	95% Adjusted-CLT UCL (Chen-1995)	1.096
		95% Modified-t UCL (Johnson-1978)	1.099

**Gamma GOF Test**

A-D Test Statistic	1.524	<b>Anderson-Darling Gamma GOF Test</b>	
5% A-D Critical Value	0.745	Data Not Gamma Distributed at 5% Significance Level	
K-S Test Statistic	0.218	<b>Kolmogorov-Smirnov Gamma GOF Test</b>	
5% K-S Critical Value	0.157	Data Not Gamma Distributed at 5% Significance Level	

**Data Not Gamma Distributed at 5% Significance Level**

**Gamma Statistics**

k hat (MLE)	20.22	k star (bias corrected MLE)	18.29
Theta hat (MLE)	0.0511	Theta star (bias corrected MLE)	0.0565
nu hat (MLE)	1254	nu star (bias corrected)	1134
MLE Mean (bias corrected)	1.034	MLE Sd (bias corrected)	0.242
Adjusted Level of Significance	0.0413	Approximate Chi Square Value (0.05)	1057
		Adjusted Chi Square Value	1053

**Assuming Gamma Distribution**

95% Approximate Gamma UCL (use when n>=50))	1.109	95% Adjusted Gamma UCL (use when n<50)	1.113
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Lognormal GOF Test		Shapiro Wilk Lognormal GOF Test	
Shapiro Wilk Test Statistic	0.776	Data Not Lognormal at 5% Significance Level	
5% Shapiro Wilk Critical Value	0.929	Lilliefors Lognormal GOF Test	
Lilliefors Test Statistic	0.242	Data Not Lognormal at 5% Significance Level	
5% Lilliefors Critical Value	0.156		

**Data Not Lognormal at 5% Significance Level**

Lognormal Statistics			
Minimum of Logged Data	-1.019	Mean of logged Data	0.00813
Maximum of Logged Data	0.464	SD of logged Data	0.244

Assuming Lognormal Distribution			
95% H-UCL	1.123	90% Chebyshev (MVUE) UCL	1.175
95% Chebyshev (MVUE) UCL	1.238	97.5% Chebyshev (MVUE) UCL	1.325
99% Chebyshev (MVUE) UCL	1.495		

**Nonparametric Distribution Free UCL Statistics**  
**Data do not follow a Discernible Distribution (0.05)**

Nonparametric Distribution Free UCLs			
95% CLT UCL	1.097	95% Jackknife UCL	1.099
95% Standard Bootstrap UCL	1.096	95% Bootstrap-t UCL	1.099
95% Hall's Bootstrap UCL	1.104	95% Percentile Bootstrap UCL	1.095
95% BCA Bootstrap UCL	1.093		
90% Chebyshev(Mean, Sd) UCL	1.149	95% Chebyshev(Mean, Sd) UCL	1.201
97.5% Chebyshev(Mean, Sd) UCL	1.273	99% Chebyshev(Mean, Sd) UCL	1.415

Suggested UCL to Use			
95% Student's-t UCL	1.099	or 95% Modified-t UCL	1.099

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. Recommendations are based upon data size, data distribution, and skewness. These recommendations are based upon the results of the simulation studies summarized in Singh, Maichle, and Lee (2006). However, simulations results will not cover all Real World data sets; for additional insight the user may want to consult a statistician.

**Note: For highly negatively-skewed data, confidence limits (e.g., Chen, Johnson, Lognormal, and Gamma) may not be reliable. Chen's and Johnson's methods provide adjustments for positively skewed data sets.**